

Problem Set 4  
IMMERSE 2005 Analysis Course

1. Prove that every compact metric space has a countable dense subset (i.e. is *separable*).
2. Prove that equivalent metrics on a metric space  $X$  will have the same convergent sequences and the same Cauchy sequences.
3. Prove that the Cantor ternary set is closed and totally disconnected.